## WRITING ASSIGNMENT 1, 18.100C

**Submission details.** A draft (at least one page) is due on Stellar by 11:59P.M. Tuesday, September 13. Your final version (2-3 pages) is due on Stellar by 11:59P.M. Thursday, September 15.

**Goal.** In order to do mathematics, we must first define our primary concepts. In this assignment, you will create several precise definitions of an ambiguous intuitive concept and then contrast your definitions by comparing their mathematical consequences.

Assignment. Create at least two precise definitions of the notion of a gap in an ordered set and discuss the advantages and disadvantages of each. As you do so, it will be helpful to examine several examples of ordered sets (e.g.,  $\mathbb{Z}$ ,  $\mathbb{R}$ ,  $(-\infty, 0] \cup (1, \infty)$ , etc.): provide rigorous proofs for the statements you make about your definitions and examples. One of your examples should be the set  $\mathbb{Q}$  of rational numbers (with its standard order); one of your definitions should identify  $\mathbb{Q}$  as having gaps, while another should identify  $\mathbb{Q}$  as gapless. You are invited to invent names for the properties you define, in which case you should try to make a good choice of terminology.

Your audience is a peer, such as an undergraduate student at MIT who has not taken and is not taking 18.100. Your writing should be clear, precise and unambiguous, but shouldn't be so technical that only someone taking 18.100 could follow it.

Technical details. Write your paper in LATEX and define and use appropriate theorem environments for your definitions and propositions. You should use the amsart document class with 11-point font (as in the template .tex file on Stellar). Do not alter the default margins. A good paper should be approximately two full pages long, and it is absolutely forbidden to exceed three pages. You are welcome to cite useful definitions or theorems from Rudin, in which case you should include a simple bibliography.

Submit your .tex file and a compiled .pdf file through Stellar for both your draft and final version. Your grade will be based on clarity of exposition, mathematical correctness, and readability of IATEX in the final version of your paper. The assignment is worth 20 points. Your draft will not be graded, but failure to submit at least one page of a draft will cap your total possible points at 10.